

Ice-breaker talk

David de Laat (ICERM/MIT)

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Generalize techniques from combinatorial optimization for packing and energy minimization problems

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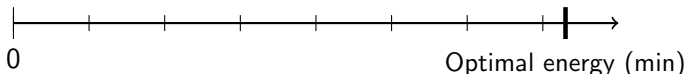
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- ▶ Example: Sharp (with high precision numerics) relaxation for Riesz energy problems with 5 particles on S^2 (2017)

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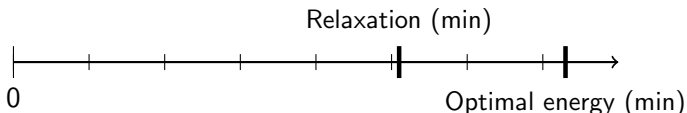
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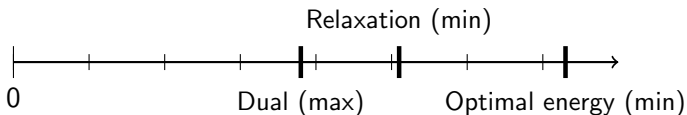
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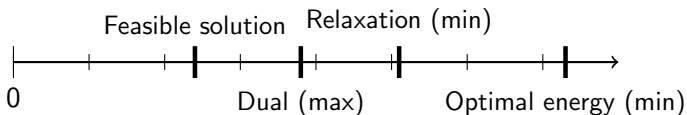
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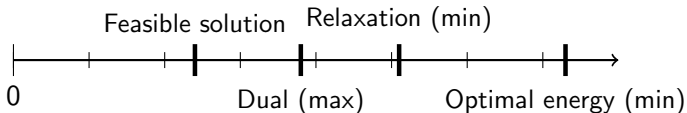
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- ▶ Current problem: Try to find stronger relaxations for sphere packing (noncompact!)

- ▶ Maximize *center density* $\limsup_{r \rightarrow \infty} |P \cap B_r| / \text{vol}(B_r)$ over sphere packings P in \mathbb{R}^n consisting of unit diameter spheres

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$$\inf \left\{ f(0) : f \in S(\mathbb{R}^n), \hat{f}(0) = 1, \hat{f} \geq 0, f(x) \leq 0 \text{ for } \|x\| \geq 1 \right\}$$

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- ▶ Copositive formulation for sphere packing:

$$\inf \left\{ f(0) + g(0) : f, g \in S(\mathbb{R}^n), \hat{f}(0) = 1, \hat{f} \geq 0, \right. \\ \left. g \text{ is copositive, } f(x) + g(x) \leq 0 \text{ for } \|x\| \geq 1 \right\}$$

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- ▶ Three point bound (only for Lattice packings):

$$\inf \left\{ f(0,0) : f \in S(\mathbb{R}^{2n}), \hat{f}(0,0) = 1, \hat{f} \geq 0, f \leq 0 \text{ on } C_2 \right\}^{1/2}$$

$$C_2 = \{(x, y) \in \mathbb{R}^{2n} : \|x\|, \|y\|, \|x - y\| \in \{0\} \cup [1, \infty)\} \setminus \{(0, 0)\}$$