

New bounds for spherical two-distance sets and equiangular lines.

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The set of points in a metric space is called an s -distance set if pairwise distances between these points admit only s distinct values. Two-distance spherical sets with the set of scalar products a and $-a$, are called equiangular. The problem of determining the maximal size of s -distance sets in various spaces has a long history in mathematics. We determine a new method of bounding the size of an s -distance set in two-point homogeneous spaces via zonal spherical functions. This method allows us to prove that the maximum size of a spherical two-distance set in n dimension Euclidean space is $n(n+1)/2$ with possible exceptions for some $n=(2k+1)^2-3$, where k is a positive integer. We also prove the universal upper bound $2/3 n a^2$ for equiangular sets with angle $1/a$ and, employing this bound, prove a new upper bound on the size of equiangular sets in an arbitrary dimension.