

High dimensional integration - the Quasi-Monte Carlo way

Frances Kuo, School of Mathematics and Statistics, UNSW Sydney, Australia

High dimensional problems - meaning problems with hundred or thousands or even infinitely many continuous variables - are now arising in many real world applications. They present major challenges to computational resources, and require serious mathematical efforts in devising new and effective methods. This talk will begin with a contemporary review of Quasi-Monte Carlo (QMC) methods, which offer tailored point constructions for solving high dimensional integration and approximation problems by sampling. By exploiting the smoothness properties of the underlying mathematical functions, QMC methods can achieve higher order convergence rates than standard Monte Carlo sampling, and moreover, QMC error bounds can be independent of the dimension under appropriate theoretical settings.

In recent years the modern QMC theory has been successfully applied to a number of application areas including option pricing in financial mathematics, maximum likelihood estimation in statistics, and PDEs with random coefficients in computational physics and uncertainty quantification. This talk will showcase some of these results as well as ongoing works where we take QMC methods to new territories such as neutron transport as a high dimensional PDE eigenvalue problem, and high frequency wave scattering in random media.